More Practical Application of Trust Management Credentials

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Abstract—Trust management is an approach to access control in distributed open systems, where access control decisions are based on policy statements made by multiple principals. The family of Role-based Trust management languages (RT) is an effective means for representing security policies and credentials in decentralized, distributed, large scale access control systems. It provides a set of role assignment credentials. A credential provides information about the privileges of users and the security policies issued by one or more trusted authorities. The main purpose of this paper is to show how extensions can make the RT family languages more useful in practice. It shows how security policies can be made more realistic by including timing information, maintaining the procedure or parameterizing the validity of credentials.

I. INTRODUCTION

The modern human life is heavily reliant on trust. The complexity of tasks we are dealing with makes it practically impossible to succeed without delegating some of them. It is therefore not surprising that the issue of trust became a very active area of research quite long ago. The trust between humans has been thoroughly analysed both from the social sciences and economic point of view, as it is an important enabler of delegation. Attempts to transfer the concept of trust to different domains were made by computer scientists, including security, electronic commerce, semantic web or even social networks areas. In any network, be it computer or social one, trust remains an essential factor. The definition of trust is however not perfectly clear, different authors show slightly different definitions. Most often it is defined either on the basis of personal experience, reputation or recommendation.

The concept of trust is closely related to the notion of reputation – the opinion about a person held by others, e.g. the opinion about an Internet seller by his customers or the opinion about the behavior of a node in a wireless sensor network built by other nodes as a result of previous interactions. Reliability is another concept related to trust. Originally, this was a measure of the length of the period during which a machine can be considered trustworthy. In general, trust can be presented a derivation of an entity’s reputation.

Access control systems, based on traditional access control models (like Mandatory Access Control (MAC), Discretionary Access Control (DAC) and Role Based Access Control (RBAC)), are in essence identity based. Authorization decisions are based entirely on the role or – more directly – identity of the requesting party and can only be made if the requester is known to the owner of the resource. The decision is based on the relation of the only two entities involved – the owner of the protected resource, who is responsible for granting access, and the requester, who requires access.

In closed, centralized environments this approach is actually correct. As identity of the users of the system is established in advance, basing access decisions on it is a natural and easy to implement choice. Unfortunately this scenario does not scale well as the system becomes decentralized and highly distributed over a network. In such open systems the set of users is not only large, but may change dynamically, leading to entirely new challenges, such as the problem of propagation of information about the changes. A central database of user’s identities is only a partial solution – although it enables the implementation of classic approaches to access control, it also introduces a single point of failure, where temporary lack of access to the central database makes any authorization decisions impossible system-wide. In absence of such a central identity repository it is no longer possible to assume that the identities of the requester and the resource owner are mutually recognized. A more flexible approach is needed, one which enables requesters to cross security domains and access resources owned by non-related entities. One such solution is called trust management.

Consider a simple example of a bookstore which offers special discounts to returning customers who are students. There is no obvious way to determine whether a given customer is eligible based only on his/her identity. Requesting a proof of identity will not resolve this problem. On the other hand, the problem can be solved efficiently using credentials, such as a bookstore card and a student card. The access rights are then determined not based on the users identity, but on the sufficiently documented information about the user’s privileges assigned by other authorities and trust for those authorities. This requires a new, different approach to access control.

The rest of this paper is organized as follows. Trust management concept is shown in Section II and Role-based Trust management family of languages is shown in Section III. Section IV presents the Role-based Trust management language syntax with an example of $RT^T$ credentials. Inference system over $RT^T$ language is described in Section V. Section VI describes a few extensions of $RT^T$ language (time validity and determination of the order). Section VII shows an inference system over new $RT^T_\infty$ language time constraints. Final
II. TRUST MANAGEMENT

Trust management was first introduced as a term by Blaze et al. [2] in 1996. The term was defined as a unified approach to specify and interpret security policies, credentials and trust relationships. The privileges of an entity in such a system are based not on its identity, but on its attributes. Multiple principals have the right to issue credentials which are then used to demonstrate the entity’s attributes. The definition of a credential is an attestation of authority, competence or qualification of an individual issued by a third party. The information contained in a credential includes privileges of a given user and/or security policies issued by trusted authorities. Real life examples of credentials are easy to propose – all sorts of academic diplomas, driver’s licenses, identification documents, certificates or membership cards are clearly credentials. In fact, a real-life credential does not need to be a document in the traditional sense of the world – e.g. keys can be treated as a form of credential. In a computer system credentials may either be records available from one or more repositories, or – more flexibly – digitally signed documents which can be provided by the requester on demand. In the first case trust for the credential follows from trust for the repository and its own access control, in the second case it is provided by the signature, obviously requiring a trusted method of propagation or verification of public keys.

In literature, the earliest described example of a trust management application was PolicyMaker [3]. An assertion language defined in this system was capable of expressing locally trusted policy statements, as well as credentials requiring a digital signature using a private key. The second generation of trust management languages includes SPKI/SDSI [6], an enhanced version of PolicyMaker called KeyNote [4] and several other languages [7]. In these languages the privileges were still assigned directly to entities and delegation of permissions through credentials was performed only directly from the issuer to the subject. This generation still did not provide any mechanism enabling delegation to be separated from identity of the entity. Introduction of delegation based on attributes (as opposed to identity) was introduced in the next generation, represented by a family of Role-based Trust management (RT) languages [8], [16], [17]. Security policies are represented by defining a formalism using credentials to establish trust in distributed, decentralized access control systems.

III. ROLE-BASED TRUST MANAGEMENT FAMILY LANGUAGES

The family of Role-based Trust management languages is used for representing security policies and credentials in decentralized, distributed access control systems. Several types of role assignment credentials are provided in RT languages, depending on the language. $RT_0$ [17] forms the core of the family, providing basic abilities – localization of authority for roles, delegation of that authority, role hierarchies and role intersections. These features are available in all RT languages, who extend this set with new features. To represent relationships between entities, parametrized roles were introduced in $RT_1$. To provide similar flexibility for resources as that provided for entities by roles, $RT_2$ extends $RT_1$ with the notion of logical objects, enabling simple assignment of access rights for entire groups of logically related objects (resources). Note that both extensions presented so far do not actually change the expressive power of the language. They allow much more concise notation, but the same policy can in fact be expressed in $RT_0$, although with a much larger set of credentials, mapping each combination of parameters or each real instance of logical objects to a separate role. The first language actually adding new capabilities not present in other members of the family is the $RT^P$ language, the main focus of this paper. The new capabilities include the ability to express agreement of multiple principals, even from disjoint sets, via manifold roles and separation of duties or threshold policies, via role-product operators.

A manifold role differs from a normal (singleton) role as instead of defining a set of principals, it defines a set of sets of principals. It is a wider term, since a singleton role can be expressed as a manifold role, whose principal sets are singletons, effectively meaning that cooperation is required from a group consisting of a single entity. Therefore, introduction of manifold roles does not affect the ability to express $RT_0$ credentials in the $RT^T$ language.

A threshold policy is used to specify a common occurrence, where agreement of multiple principals is required to initiate a given action. More formally, at least $k$ entities from a set satisfying certain conditions must agree on some fact. E.g. in banking certain transactions require authorisation by two cashiers. Separation of duties policy is similar, but the agreeing entities fulfill different roles (e.g. in the banking example some transactions may also require authorisation by a controller). Both types of policies specify requirements that cannot be fulfilled by a single entity and therefore cannot be expressed in $RT_0$.

The RT family includes one more important language, $RT^P$, which provides mechanisms to describe delegation of role activations and selective use of role membership. However, this language is out of scope of this paper. More in-depth information about the RT family of languages can be found in paper [16].

The main advantage of trust management approach is the ability to use delegation. A principal’s authority over a resource may be transferred in a limited fashion to other principals by simple means of a credential. The notion of ownership is no longer central – the access control strategy and all decisions on who is authorized to use which resource is defined by a set of credentials. One upside of such approach is that the authority is easy to transfer over a network – as long as a credential can be transferred and trusted in another location, there is no need to involve the identity of the resource owner. However, although such decentralization of credential storage is very useful, it does present a variety of new problems.

In the years since its creation, the concept of trust man-
management has evolved significantly, made applicable to new, broader contexts, such as assessment of reliability or trustworthiness of systems and individuals [15]. In this paper we restrict the meaning of trust management only to its original context of access control. A lot of different work connected with the possibility of using RT in different types of network, eg. Role based Trust management model for Peer-to-Peer networks [5], a trust management system for Ad-Hoc Networks [1], or Wireless Sensor Networks [11], and also Role-based Trust Management Model in Multi-domain Environment [18] have been studied recently.

Our approach is another type of extension of trust management languages. It shows how to make RT family languages more useful in practice by including time validity constraints and order of entities which can appear in the execution context.

IV. THE SYNTAX OF RT FAMILY LANGUAGES

RT languages use a set of basic elements, such as entities, role names, roles and credentials. Entities are principals controlling access to resources by defining roles and issuing credentials as well as requesters willing to access resources. The entity may be a person, but it might just as well be an application, identifying itself in a computer system by a user name or a public key. Role names represent permissions and can be issued to entities or groups of them by other entities. Roles represent sets of entities for which the access control policies grant particular permissions. Credentials define roles by appointing a new member of the role or by delegating authority to members of other roles. RT includes six different types of credentials, the first four in common with the less expressive RT languages:

\[
\begin{align*}
A.r & \leftarrow B & \text{simple membership: entity } B \text{ is a member of role } A.r, \\
A.r & \leftarrow B.s & \text{simple inclusion: role } A.r \text{ includes (all members of) role } B.s. \text{ This type of credential involves delegation of authority over role } r, \text{ since by issuing new credentials defining } B.s \text{ role } B.s \text{ may add new members to role } A.r. \text{ This type of credential is also used to define role hierarchies.} \\
A.r & \leftarrow B.s.t & \text{linking inclusion: role } A.r \text{ includes role } C.t \text{ for each } C, \text{ which is a member of role } B.s. \text{ This is a delegation of authority from } A \text{ to all the members of the role } B.s. \text{ The expression } B.s.t \text{ is called a linked role.} \\
A.r & \leftarrow B.s \cap C.t & \text{intersection inclusion: role } A.r \text{ includes all members of both roles } B.s \text{ and } C.t. \text{ This is a partial delegation from } A \text{ to } B \text{ and } C. \text{ The expression } B.s \cap C.t \text{ is known as an intersection role.}
\end{align*}
\]

Since the models used in practice can be very complex, this paper uses some simplified examples. We focus on RT-specific credentials and intend to illustrate the basic notions and notation, not the full expressive power of the language.

**Example 4.1 (Example of RT - subject):**

Suppose that a university will only activate a subject if at least two of four students apply and among the applicants at least one is a PhD student. RT would require a long list of credentials listing all possible satisfactory combinations, changed whenever the list of students changes. RT allows us to express this rule as just two policy credentials and a list of simple membership credentials, easy to manage along with the official list of students. The policy credentials are:

\[
\begin{align*}
F.students & \leftarrow F.student \circ F.student \\
F.activeSubject & \leftarrow F.students \circ F.phdStudent
\end{align*}
\]

Now, if the following membership credentials are added:

\[
\begin{align*}
F.student & \leftarrow \{Alex\} \\
F.student & \leftarrow \{Betty\} \\
F.student & \leftarrow \{David\} \\
F.student & \leftarrow \{John\} \\
F.phdStudent & \leftarrow \{John\} \\
F.phdStudent & \leftarrow \{Emily\}
\end{align*}
\]

we can conclude that any pair of students from the set \{Alex, Betty, David, John\} fulfills the role F.students and that the subject can be activated if the pair includes John or if Emily is willing to attend.

**Example 4.2 (Example of RT - signature):** Suppose that we have a situation in which we need to collect the signatures of the requester, accountant, his official superior, the manager of financial department and the director of a company to accept some transaction. Such a policy can be described using the following credentials:

\[
\begin{align*}
\circ \text{Company.signature} & \leftarrow \text{Company.requester} \\
\circ \text{Company.accountant} & \circ \text{Company.superior} \\
\circ \text{Company.fdManager} & \circ \text{Company.director}
\end{align*}
\]

Now suppose that we have such people, who play those roles, so the following credentials have been added to our security policy:

\[
\begin{align*}
\text{Company.requester} & \leftarrow \{Jacob\}
\end{align*}
\]
As we can see, to complete the set of signatures we need just two people: Jacob, who can play a role of requestor, accountant, fdManager and William who plays the role of superior and director, but as may be required, groups of people \{Jacob, Eliot, William\}, \{Jacob, Eliot, Michael, William\}, \{Jacob, Alexander, William\}, and \{Jacob, Alexander, Michael, William\} can also play a manifold role, and cooperatively complete the set of signatures.

V. Inference System over RT^T Credentials

RT^T credentials define roles, which in turn are used to represent permissions. The set of member entities for a role is defined by a set \( P \) of RT^T credentials. This set can be more conveniently calculated using an inference system, which defines an operational semantics of RT^T language. The system consists of a set of inference rules used to derive credentials from existing ones and an initial set of formulae.

The system must be sound and complete. Soundness guarantees that any valid formula is derivable. Completeness is proved by showing that every formula \( P \models A.r \rightarrow X \) can be derived using inference rules for each element \((A,r,X)\) of \( S_P \). Both proofs can be found in \cite{10}, showing that the inference system is a valid alternative way of presenting the semantics of RT^T.

Example 5.1 (Inference system for Example 4.1):

We will now derive the set of entities that can cooperate to activate a subject using an inference system, using a limited set of credentials for brevity: ((1), (2), (4), (6), and (7)). Using credentials (1), (2), (4), (6), and (7) according to rule (W_1) we can infer:

\[
\begin{align*}
F.\text{students} &\rightarrow F.\text{student} \otimes F.\text{student} \in P \\
\neg P &\models F.\text{students} \otimes F.\text{student} \\
F.\text{activeSubject} &\rightarrow F.\text{students} \otimes F.\text{phdStudent} \in P \\
\neg P &\models F.\text{activeSubject} \otimes F.\text{students} \otimes F.\text{phdStudent} \\
F.\text{student} \rightarrow \{\text{Betty}\} &\in P \\
\neg P &\models F.\text{student} \rightarrow \{\text{Betty}\} \\
F.\text{student} \rightarrow \{\text{John}\} &\in P \\
\neg P &\models F.\text{student} \rightarrow \{\text{John}\} \\
F.\text{phdStudent} \rightarrow \{\text{John}\} &\in P \\
\neg P &\models F.\text{phdStudent} \rightarrow \{\text{John}\}
\end{align*}
\]

Then, using credentials (1), (6) and (4) and rule (W_6) we infer:

\[
\begin{align*}
\neg P &\models F.\text{students} \rightarrow \{\text{John}, \text{Betty}\} \\
F.\text{students} &\rightarrow F.\text{student} \otimes F.\text{student} \\
\neg P &\models F.\text{students} \rightarrow F.\text{student} \\
\neg P &\models F.\text{students} \rightarrow \{\text{John}\} \\
\neg P &\models F.\text{students} \rightarrow \{\text{John}\} \\
F.\text{phdStudent} &\rightarrow \{\text{John}\} \\
\neg P &\models F.\text{phdStudent} \\
F.\text{student} &\rightarrow \{\text{Betty}\} \\
\neg P &\models F.\text{student} \\
F.\text{student} &\rightarrow \{\text{Betty}\} \\
\neg P &\models F.\text{students} \rightarrow \{\text{John}, \text{Betty}\} \\
\neg P &\models F.\text{students} \rightarrow \{\text{John}, \text{Betty}\}
\end{align*}
\]

These newly inferred credentials (2) and (7) with the rule (W_5):

\[
\begin{align*}
\neg P &\models F.\text{activeSubject} \rightarrow F.\text{students} \otimes F.\text{phdStudent} \\
\neg P &\models F.\text{activeSubject} \rightarrow \{\text{John}\} \\
\neg P &\models F.\text{students} \rightarrow \{\text{John}, \text{Betty}\}
\end{align*}
\]

we can show that the set of entities \{John, Betty\} is sufficient to activate the subject.
Example 5.2 (Inference system for Example 4.2): We use the inference system to formally derive a set of entities who are essential to accept some transaction, i.e. the signatures of the requester, accountant, his official superior, the manager of financial department and the director of a company. To make the notation shorter, let us use $C$ instead of Company.

Using credentials (9)-(17) according to the rule ($W_1$) we can infer:

$$C.\text{signature} \leftarrow C.\text{requester}$$
$$C.\text{accountant} \leftarrow \{\text{Jacob}\} \in P$$
$$P \succ C.\text{accountant} \leftarrow \{\text{Jacob}\}$$
$$C.\text{accountant} \leftarrow \{\text{Eliot}\} \in P$$
$$P \succ C.\text{accountant} \leftarrow \{\text{Eliot}\}$$
$$C.\text{accountant} \leftarrow \{\text{Michael}\} \in P$$
$$P \succ C.\text{accountant} \leftarrow \{\text{Michael}\}$$
$$C.\text{director} \leftarrow \{\text{William}\} \in P$$
$$P \succ C.\text{director} \leftarrow \{\text{William}\}$$

Then, using credentials (9), (10), (11), (14), (16) and (17) and rule ($W_5$) we infer:

$$P \succ C.\text{signature} \leftarrow C.\text{requester}$$
$$P \succ C.\text{accountant} \leftarrow \{\text{Jacob}\}$$
$$P \succ C.\text{superior} \leftarrow \{\text{William}\}$$
$$P \succ C.\text{director} \leftarrow \{\text{William}\}$$

showing that here we need four people to complete the set of signatures, i.e. $\{\text{Jacob, Eliot, William}\}$.

Or, using credentials (9), (10), (12), (14), (16) and (17) and rule ($W_5$) we infer:

$$P \succ C.\text{signature} \leftarrow C.\text{requester}$$
$$P \succ C.\text{accountant} \leftarrow \{\text{Jacob}\}$$
$$P \succ C.\text{superior} \leftarrow \{\text{William}\}$$
$$P \succ C.\text{director} \leftarrow \{\text{William}\}$$

showing that here we need more people to complete the set of signatures, i.e. $\{\text{Jacob, Eliot, William}\}$.

Depending on which credentials at the moment we have (because not all the credentials are always available), we can determine the sets of people who can cooperatively sign the document.

VI. CREDENTIAL EXTENSIONS

This section shows a few extensions of $RT^T$ languages which make it more useful in practice.

A. Time Validity in $RT^T$

Real security policies involve time restrictions. Allowing the credentials to have limited time validity can make the $RT^T$ language more useful in practice. Inference rules with time validity for $RT_0$ were originally introduced in a slightly different way in [14]. In [13] we tried to extend the potential of $RT^T$ language by adding time validity constraints. Most permissions are in fact given for fixed periods of time, permanent permissions are less common. Time dependent credentials take the form: $c \in v$, meaning "the credential $c$ is available during the time $v"$. Finite sets of time dependent credentials are denoted by $\overline{CP}$ and the new language is called $RT^T_c$. $c$ is used to denote "$c$ in $(-\infty, +\infty)$" to make notation lighter.

Most trust management languages are monotonic: adding new assertion to a query can never result in canceling an action, which was accepted before [9]. Therefore, each policy statement or credential added to the system may only increase the capabilities and privileges granted to others, making revocation of rights impossible. Introduction of time
constraints does not invalidate the monotonicity of the system, but achieves some of the utility of negation.

Time validity can be denoted as follows:

\[ [\tau_1, \tau_2]; [\tau_1, \tau_2]; (\tau_1, \tau_2); (\infty, \tau); (-\infty, \tau); [\tau, +\infty); (\tau, +\infty); (-\infty, +\infty); \tau \cup \tau_2; \tau \cap \tau_2; \tau \setminus \tau_2 \]

and \( \tau \) ranging over time constants.

Example 6.1 (Time validity for Example 4.1):
Assuming that Alex, Betty, David and John in our scenario will not be student forever seems quite natural. John and Emily’s PhD student status is similar. Thus, credentials (3)–(8) should be generalized to:

\[
\begin{align*}
F.student & \leftarrow \{Alex\} \text{ in } v_1 \\
F.student & \leftarrow \{Betty\} \text{ in } v_2 \\
F.student & \leftarrow \{David\} \text{ in } v_3 \\
F.student & \leftarrow \{John\} \text{ in } v_4 \\
F.phdStudent & \leftarrow \{John\} \text{ in } v_5 \\
F.phdStudent & \leftarrow \{Emily\} \text{ in } v_6
\end{align*}
\]

stating that (3) – (8) are only available during \( v_1, v_2, v_3, v_4, v_5, \) and during \( v_6 \), respectively. The policy itself, described by credentials (1) and (2) may however be permanent. By using (1), (2) and (18)–(23), we want to be able to derive that for example the set \{Jacob, William\} can cooperatively activate the subject during all of the period: \( v_1 \cap v_2 \cap v_3 \cap v_7 \cap v_8 \), where Jacob plays the role of requester, accountant and financial department manager and William acts as a superior and director of the company. But during the time \( v_1 \cap v_3 \cap v_5 \cap v_7 \cap v_8 \) it has to be the set consisting of \{Jacob, Eliot, Michael, William\}.

While in both examples the policy defining credentials were assumed to be permanently valid, this is not required. Some policies are naturally time-limited (eg. seasonal sales).

B. Determination of the order

Another powerful feature which would be useful to model more realistic policies is the ability to determine the order in which a member of a role or an entity (entities) can appear.

If we want to maintain a procedure, we have to add two new types of credentials at the syntax level. These are:

\[
A.r \leftarrow B.s_\cap C.t
\]

– role \( A.r \) is satisfied by a union set of one member of role \( B.s \) and one member of role \( C.t \) in this exact order or by one entity satisfying the intersection role \( B.s \cap C.t \).

\[
A.r \leftarrow B.s \cup C.t
\]

– role \( A.r \) is satisfied by a set of two different entities: one member of role \( B.s \) and one member of role \( C.t \) in this order.

In our Example 4.1 we can want to have such situation:

\[
F.activeSubject \leftarrow F.students_\cap F.phdStudent
\]

which means that the order is important. First we need to have two students and just after that one PhD student.

That extension can be extremely useful in a large variety of situations. For example, if we have a situation, when one person is a member of a few roles, it can be useful to have some restrictions connected with appearing in particular roles during the execution context when the credential is used.

Example 6.3 (The right order of signature):
When we have a situation in which we need to collect the signatures of people who are essential to accept some transaction, we can imagine at least a few scenarios in our security policy.

Suppose that we need a signature of the requester, accountant, his official superior, the manager of financial department and the director of a company, in such order.

Now we can use the data from Example 4.2 and we can have three different scenarios:

1) The order is strictly obeyed and it is important that an accountant can give his signature after having
received the signature of a requester, and accountant’s superior can give his signature after having received the signature of an accountant, even if it is one person. This means that in a first step Jacob can sign the document as a requester, in a second step as an accountant, after that William can give his signature as a Jacob’s official superior. In the next step Jacob can sign the document as a financial department manager, and at the end William can sign the document as a director of the company. Table I presents the signature order in our first scenario.

It can be important in some situation to strictly keep the order of signatures, but in a huge implementation it can be a little bit inefficient. That is why we can propose two other scenarios.

2) We can allow signing the document by one person who plays a few roles at once if the roles appear in credentials successively without any role between. In our example it can look like in the Table II (to make our example easier, we can use just credentials (10), (11), (14), (16), (17)).

In such a simple example, we have one step less than in the previous scenario. It shows how such change can be useful in real large systems.

3) In our third scenario we can allow that one person, who plays more than one role, can give all the signatures at once. It can be very useful in an automatic implementation. Table III shows how it can look in our third scenario.

That situation means that Jacob accepts his signature as a financial department manager if William signs the document as his official superior and William accepts his signature as a director if Jacob signs the document as a financial department manager. We have to have a possibility to accept or not accept our signature, which is dependent on another person’s signature.

If we want to mandate that the entity can appear in particular roles during the execution context exactly when the credential is used, we can put a new type of role denoted by underlined identifiers (e.g. $\underline{\text{director}}$). In such situation, when we change the credential:

$\text{Company.signature} \xleftarrow{\underline{\text{director}}} \text{Company.requester}$
$\text{Company.accountant} \xleftarrow{\underline{\text{director}}} \text{Company.superior}$
$\text{Company.jdManager} \xleftarrow{\underline{\text{director}}} \text{Company.director}$

into:

$\text{Company.signature} \xleftarrow{\underline{\text{director}}} \text{Company.requester}$
$\text{Company.accountant} \xleftarrow{\underline{\text{director}}} \text{Company.superior}$
$\text{Company.jdManager} \xleftarrow{\underline{\text{director}}} \text{Company.director}$

in our third scenario we will have the situation described in Table IV, meaning that William has to wait with his signature as a director until the time Jacob approves his signature as $\text{fdManager}$.

All the semantics previously defined for $RT^T_+$, set-theoretic (which maps roles to a set of entity names), operational semantics (where credentials can be derived from the initial set of credentials using a set of inference rules [13]), and logic-programming (where credentials are translated into a logic program [12]), are still valid, meaning that proofs of the soundness and the completeness of those semantics are also valid.

This section shows how we can explore the potential of RT languages. It shows how security policies can be made more realistic by including timing information or maintaining the procedure.

VII. INFERENCE SYSTEM FOR $RT^T$ CREDENTIALS WITH TIME VALIDITY

All the semantics previously defined for RT languages are still valid for determined order, but they have to be changed for credentials with time validity. Because of that reason we have to take on it. This section is showing an inference system for $RT^T$ credentials with time validity.

We will now adapt the inference system over $RT^T$ credentials to respect time validity. Let $CP$ be a set of $RT^T$ credentials, from which new credentials may be derived. A derived credential $c$ valid in time $\tau$ will be denoted using a formula $CP \succ_{\tau} c$, meaning that the credential $c$ can be derived from a set of credentials $CP$ during the time $\tau$. The initial set of formulae of an inference system over a set $CP$ of $RT^T_+$ credentials are all the form: $c \in v \in CP$ for each credential $c$ valid in time $\tau$ in $CP$. The inference rules of the system are the following:

$\frac{c \in v \in CP \quad \tau \in v}{CP \succ_{\tau} c}$ (CW1)

$\frac{CP \succ_{\tau} A.r \leftarrow B.s \quad CP \succ_{\tau} B.s \leftarrow X}{CP \succ_{\tau} A.r \leftarrow X}$ (CW2)

$\frac{CP \succ_{\tau} A.r \leftarrow B.s.t \quad CP \succ_{\tau} B.s \leftarrow C}{CP \succ_{\tau} C.t \leftarrow X}$

$\frac{CP \succ_{\tau} C.t \leftarrow X \quad CP \succ_{\tau} A.r \leftarrow X}{CP \succ_{\tau} A.r \leftarrow X \lor Y}$ (CW3)

$\frac{CP \succ_{\tau} A.r \leftarrow B.s \cap C.t \quad CP \succ_{\tau} B.s \leftarrow X}{CP \succ_{\tau} C.t \leftarrow X}$

$\frac{CP \succ_{\tau} C.t \leftarrow X \quad CP \succ_{\tau} A.r \leftarrow X}{CP \succ_{\tau} A.r \leftarrow X \lor Y}$ (CW4)

$\frac{CP \succ_{\tau} A.r \leftarrow B.s \cap C.t \quad CP \succ_{\tau} B.s \leftarrow X}{CP \succ_{\tau} C.t \leftarrow Y \quad X \lor Y = \phi}$ (CW5)

$\frac{CP \succ_{\tau} C.t \leftarrow Y \quad X \lor Y = \phi}{CP \succ_{\tau} A.r \leftarrow X \lor Y}$ (CW6)

All the derived credentials either belong to set $CP$ (rule CW1) or are of the type: $CP \succ_{\tau} A.r \leftarrow X$ (rules CW2 through CW6). This new inference system is based on an extension of the inference rules from section V, where rules
TABLE I
Signature order in the first scenario

<table>
<thead>
<tr>
<th>Step</th>
<th>requester</th>
<th>accountant</th>
<th>superior</th>
<th>fdManager</th>
<th>director</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Jacob</td>
<td>φ</td>
<td>φ</td>
<td>φ</td>
<td>φ</td>
</tr>
<tr>
<td>2</td>
<td>Jacob</td>
<td>Jacob, Eliot, Alexander</td>
<td>φ</td>
<td>φ</td>
<td>φ</td>
</tr>
<tr>
<td>3</td>
<td>Jacob</td>
<td>Jacob, Eliot, Alexander</td>
<td>William, Michael</td>
<td>φ</td>
<td>φ</td>
</tr>
<tr>
<td>4</td>
<td>Jacob</td>
<td>Jacob, Eliot, Alexander</td>
<td>William, Michael</td>
<td>Jacob</td>
<td>φ</td>
</tr>
<tr>
<td>5</td>
<td>Jacob</td>
<td>Jacob, Eliot, Alexander</td>
<td>William, Michael</td>
<td>Jacob</td>
<td>William</td>
</tr>
</tbody>
</table>

TABLE II
Signature order in the second scenario

<table>
<thead>
<tr>
<th>Step</th>
<th>requester</th>
<th>accountant</th>
<th>superior</th>
<th>fdManager</th>
<th>director</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Jacob</td>
<td>Jacob</td>
<td>φ</td>
<td>φ</td>
<td>φ</td>
</tr>
<tr>
<td>2</td>
<td>Jacob</td>
<td>Jacob</td>
<td>William</td>
<td>φ</td>
<td>φ</td>
</tr>
<tr>
<td>3</td>
<td>Jacob</td>
<td>Jacob</td>
<td>William</td>
<td>Jacob</td>
<td>φ</td>
</tr>
<tr>
<td>4</td>
<td>Jacob</td>
<td>Jacob</td>
<td>William</td>
<td>Jacob</td>
<td>William</td>
</tr>
</tbody>
</table>

TABLE III
Signature order in the second scenario

<table>
<thead>
<tr>
<th>Step</th>
<th>requester</th>
<th>accountant</th>
<th>superior</th>
<th>fdManager</th>
<th>director</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Jacob</td>
<td>Jacob</td>
<td>φ</td>
<td>Jacob</td>
<td>φ</td>
</tr>
<tr>
<td>2</td>
<td>Jacob</td>
<td>Jacob</td>
<td>William</td>
<td>Jacob</td>
<td>William</td>
</tr>
</tbody>
</table>

TABLE IV
Signature order in the third "underlined" scenario

<table>
<thead>
<tr>
<th>Step</th>
<th>requester</th>
<th>accountant</th>
<th>superior</th>
<th>fdManager</th>
<th>director</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Jacob</td>
<td>Jacob</td>
<td>φ</td>
<td>Jacob</td>
<td>φ</td>
</tr>
<tr>
<td>2</td>
<td>Jacob</td>
<td>Jacob</td>
<td>William</td>
<td>Jacob</td>
<td>φ</td>
</tr>
<tr>
<td>3</td>
<td>Jacob</td>
<td>Jacob</td>
<td>William</td>
<td>Jacob</td>
<td>William</td>
</tr>
</tbody>
</table>

(W_i) are replaced with (CW_i) and only valid time-dependent credentials from CP are considered.

The proof of soundness of the inference system requires showing that for each new formula CP \succ \tau A.r \leftarrow X, the triple (A, r, X) belongs to the semantics S_CP of the set CP. All the formulae CP \succ \tau A.r \leftarrow X such that A.r \leftarrow X \in CP are sound, as shown in [12].

Completeness of the inference system over a set CP of RT^+_T credentials can be proved by showing that a formula CP \succ \tau A.r \leftarrow X can be derived using inference rules for each element (A, r, X) \in S_CP. The proof is presented in [12].

A. Inferring time validity of credentials

The proposed inference system can also derive the maximal time validity of a credential c from CP. Formula CP \succ \tau c is modified to CP \succ \tau v c, meaning that at any time \tau \in v in which CP has a semantics, it is possible to infer the credential c from CP. The inference rules of the system are the following:

\[
\frac{c \text{ in } v \in CP}{CP \succ \succ \tau v c} \quad (\text{CWP}_1)
\]

\[
\frac{CP \succ \succ \tau_{v_1} A.r \leftarrow B.s \quad CP \succ \succ \tau_{v_2} B.s \leftarrow X}{CP \succ \succ \tau_{v_1 \cap v_2} A.r \leftarrow X} \quad (\text{CWP}_2)
\]

\[
\frac{CP \succ \succ \tau_{v_2} B.s \leftarrow C \quad CP \succ \succ \tau_{v_3} C.t \leftarrow X}{CP \succ \succ \tau_{v_2 \cap v_3 \cap v_3} A.r \leftarrow X} \quad (\text{CWP}_3)
\]

\[
\frac{CP \succ \succ \tau_{v_1} A.r \leftarrow B.s \cap C.t \quad CP \succ \succ \tau_{v_3} B.s \leftarrow X \quad CP \succ \succ \tau_{v_3} C.t \leftarrow X}{CP \succ \succ \tau_{v_1 \cap v_2 \cap v_3} A.r \leftarrow X} \quad (\text{CWP}_4)
\]

\[
\frac{CP \succ \succ \tau_{v_2} B.s \leftarrow C \quad CP \succ \succ \tau_{v_3} C.t \leftarrow Y}{CP \succ \succ \tau_{v_1 \cap v_2 \cap v_3} A.r \leftarrow X \cup Y} \quad (\text{CWP}_5)
\]
valid. Rules \((\text{CP} \triangleright \triangleright v_1)\text{ A.r} \leftarrow B.s \odot C.t\) \((\text{CP} \triangleright \triangleright v_2) B.s \leftarrow X \text{ CP} \triangleright \triangleright v_3 C.t \leftarrow Y \text{ X} \cap Y = \phi\) (CWP\(_6\))

\[
\begin{align*}
\text{CP} \triangleright \triangleright v_1 \triangleright \triangleright v_2 \triangleright \triangleright v_3 A.r \leftarrow X \cap Y \\
\text{CP} \triangleright \triangleright v_1 \triangleright \triangleright v_2 C.t \leftarrow Y \\
\text{CP} \triangleright \triangleright v_3 C = \text{CP} \triangleright \triangleright v_2 c \\
\text{CP} \triangleright \triangleright v_1 \cap v_2 c 
\end{align*}
\]

(CWP\(_7\))

Rule is (CWP\(_1\)) claims that \(\text{CP}\) can be used whenever it is valid. Rules (CWP\(_2\)) - (CWP\(_6\)) simply claim that inference rules can be used iff all their premises are true. Finally, the rule (CWP\(_7\)) is used to join validity periods, meaning that if \(c\) can be inferred with validity \(v_1\) and validity \(v_2\), then it can also be inferred with validity \(v_1 \cap v_2\). \(\text{CP} \triangleright \triangleright v\) generalizes \(\text{CP} \triangleright \triangleright v\). They are both equivalent whenever \(v = [\tau, \tau]\). Note that inferring a certain \(c\) from \(\text{CP}\) may be possible in several different ways, resulting in different validity periods. Rule (CWP\(_7\)) can then be used as many times as necessary to broaden \(c\)'s validity.

Maximal inference is the process, where in each step we infer with maximal time validity.

An inference terminating in \(\text{CP} \triangleright \triangleright v\ c\) is called maximal if and only if:

1) there exists no \(v' > v\) such that \(\text{CP} \triangleright \triangleright v'\ c\), and
2) every its sub-inference terminating in \(\text{CP} \triangleright \triangleright v'\ c'\), for \(c' \neq c\) is maximal.

The first condition ensures that further use of rule (CWP\(_7\)) will not extend the validity of \(c\). The second condition ensures that this property is propagated through the whole inference tree. Maximal inferences guarantee that \(v\) in \((\text{CP} \triangleright \triangleright v_1)\) is the maximal time validity for \(A.r \leftarrow X\).

For these inferences we can prove soundness and completeness of \(\text{CP} \triangleright \triangleright v\), as shown in [12].

Example 7.1 (Time validity in inference system for Example 4.1): Let us get back to our example and to make long example shorter, let us use less credentials: (1), (2), (19), (21), and (22). According to rule (CWP\(_1\)) we can infer:

\[
\text{CP} \triangleright \triangleright v_1 \text{ F.activeSubject} \leftarrow \text{F.students} \circ \text{F.phdStudent}
\]

In next step we use it and additionally credentials (2), (22) and rule (CWP\(_5\)):

\[
\text{CP} \triangleright \triangleright \text{F.activeSubject} \leftarrow \text{F.students} \circ \text{F.phdStudent}
\]

\[
\text{CP} \triangleright \triangleright v_2 \text{ F.phdStudent} \leftarrow \{\text{Betty, John}\}
\]

\[
\text{CP} \triangleright \triangleright v_3 \text{ F.students} \leftarrow \{\text{Betty, John}\}
\]

\[
\text{CP} \triangleright \triangleright v_4 \text{ C.requester} \leftarrow \{\text{Betty, John}\}
\]

\[
\text{CP} \triangleright \triangleright v_5 \text{ C.accountant} \leftarrow \{\text{Betty, John}\}
\]

\[
\text{CP} \triangleright \triangleright v_6 \text{ C.director} \leftarrow \{\text{Betty, John}\}
\]

\[
\text{CP} \triangleright \triangleright v_7 \text{ C.requester} \leftarrow \{\text{Betty, John}\}
\]

\[
\text{CP} \triangleright \triangleright v_8 \text{ C.accountant} \leftarrow \{\text{Betty, John}\}
\]

\[
\text{CP} \triangleright \triangleright v_9 \text{ C.director} \leftarrow \{\text{Betty, John}\}
\]

\[
\text{CP} \triangleright \triangleright v_{10} \text{ C.requester} \leftarrow \{\text{Betty, John}\}
\]

\[
\text{CP} \triangleright \triangleright v_{11} \text{ C.accountant} \leftarrow \{\text{Betty, John}\}
\]

\[
\text{CP} \triangleright \triangleright v_{12} \text{ C.director} \leftarrow \{\text{Betty, John}\}
\]

\[
\text{CP} \triangleright \triangleright v_{13} \text{ C.requester} \leftarrow \{\text{Betty, John}\}
\]

\[
\text{CP} \triangleright \triangleright v_{14} \text{ C.accountant} \leftarrow \{\text{Betty, John}\}
\]

\[
\text{CP} \triangleright \triangleright v_{15} \text{ C.director} \leftarrow \{\text{Betty, John}\}
\]

\[
\text{CP} \triangleright \triangleright v_{16} \text{ C.requester} \leftarrow \{\text{Betty, John}\}
\]

\[
\text{CP} \triangleright \triangleright v_{17} \text{ C.accountant} \leftarrow \{\text{Betty, John}\}
\]

\[
\text{CP} \triangleright \triangleright v_{18} \text{ C.director} \leftarrow \{\text{Betty, John}\}
\]

\[
\text{CP} \triangleright \triangleright v_{19} \text{ C.requester} \leftarrow \{\text{Betty, John}\}
\]

\[
\text{CP} \triangleright \triangleright v_{20} \text{ C.accountant} \leftarrow \{\text{Betty, John}\}
\]

\[
\text{CP} \triangleright \triangleright v_{21} \text{ C.director} \leftarrow \{\text{Betty, John}\}
\]

\[
\text{CP} \triangleright \triangleright v_{22} \text{ C.requester} \leftarrow \{\text{Betty, John}\}
\]

\[
\text{CP} \triangleright \triangleright v_{23} \text{ C.accountant} \leftarrow \{\text{Betty, John}\}
\]

\[
\text{CP} \triangleright \triangleright v_{24} \text{ C.director} \leftarrow \{\text{Betty, John}\}
\]

\[
\text{CP} \triangleright \triangleright v_{25} \text{ C.requester} \leftarrow \{\text{Betty, John}\}
\]

\[
\text{CP} \triangleright \triangleright v_{26} \text{ C.accountant} \leftarrow \{\text{Betty, John}\}
\]

\[
\text{CP} \triangleright \triangleright v_{27} \text{ C.director} \leftarrow \{\text{Betty, John}\}
\]

\[
\text{CP} \triangleright \triangleright v_{28} \text{ C.requester} \leftarrow \{\text{Betty, John}\}
\]

\[
\text{CP} \triangleright \triangleright v_{29} \text{ C.accountant} \leftarrow \{\text{Betty, John}\}
\]

\[
\text{CP} \triangleright \triangleright v_{30} \text{ C.director} \leftarrow \{\text{Betty, John}\}
\]

\[
\text{CP} \triangleright \triangleright v_{31} \text{ C.requester} \leftarrow \{\text{Betty, John}\}
\]

\[
\text{CP} \triangleright \triangleright v_{32} \text{ C.accountant} \leftarrow \{\text{Betty, John}\}
\]

\[
\text{CP} \triangleright \triangleright v_{33} \text{ C.director} \leftarrow \{\text{Betty, John}\}
\]
showing that the set of entities \{Jacob, William\} is sufficient to complete the set of signatures during the time \(v_1 \cap v_2 \cap v_3 \cap v_5 \cap v_7 \cap v_8\).

Or, using credentials (9), (24), (26), (28), (30) and (31) and rule (CWP) we infer:

\[
\begin{align*}
\text{CP} & \triangleright \triangleright C.\text{signature} \leftarrow C.\text{requester} \\
& \quad \circ C.\text{accountant} \circ C.\text{superior} \\
& \quad \circ C.\text{fdManager} \circ C.\text{director} \\
\text{CP} & \triangleright \triangleright v_1 \circ v_2 \text{.} C.\text{requester} \leftarrow \{Jacob\} \\
\text{CP} & \triangleright \triangleright v_3 \text{.} C.\text{accountant} \leftarrow \{Eliot\} \\
\text{CP} & \triangleright \triangleright v_5 \text{.} C.\text{superior} \leftarrow \{William\} \\
\text{CP} & \triangleright \triangleright v_7 \circ v_8 \text{.} C.\text{fdManager} \leftarrow \{Jacob\} \\
\text{CP} & \triangleright \triangleright v_3 \circ v_5 \circ v_7 \circ v_8 \text{.} C.\text{director} \leftarrow \{William\}
\end{align*}
\]

showing that here we need more people to complete the set of signatures, i.e. \{Jacob, Eliot, William\} during the time \(v_1 \cap v_2 \cap v_3 \cap v_5 \cap v_7 \cap v_8\).

Or, using credentials (9), (24), (27), (29), (30) and (31) and rule (CWP) we infer:

\[
\begin{align*}
\text{CP} & \triangleright \triangleright C.\text{signature} \leftarrow C.\text{requester} \\
& \quad \circ C.\text{accountant} \circ C.\text{superior} \\
& \quad \circ C.\text{fdManager} \circ C.\text{director} \\
\text{CP} & \triangleright \triangleright v_1 \circ v_2 \text{.} C.\text{requester} \leftarrow \{Jacob\} \\
\text{CP} & \triangleright \triangleright v_3 \text{.} C.\text{accountant} \leftarrow \{Eliot\} \\
\text{CP} & \triangleright \triangleright v_5 \text{.} C.\text{superior} \leftarrow \{William\} \\
\text{CP} & \triangleright \triangleright v_7 \circ v_8 \text{.} C.\text{fdManager} \leftarrow \{Jacob\} \\
\text{CP} & \triangleright \triangleright v_3 \circ v_5 \circ v_7 \circ v_8 \text{.} C.\text{director} \leftarrow \{William\}
\end{align*}
\]

showing that here we need four people to complete the set of signatures, i.e. \{Jacob, Eliot, Michael, William\} during the time \(v_1 \cap v_2 \cap v_3 \cap v_5 \cap v_7 \cap v_8\).

VIII. CONCLUSIONS

In the paper we model the use of trust management systems in decentralized and distributed environments. The modelling framework is a family of Role-based Trust management language RT. The core part of the paper is introduction of time validity constraints and especially maintaining the procedure – modifications aimed at making the RT language more realistic. While the inference systems presented in this paper are simple, they are well-founded theoretically. The utility of the proposed extensions is most visible in large-scale distributed systems, where users have only partial view of their execution context.